

Spectral correction to recover full 10min variability from hourly mesoscale data

Presenter: Lasse Svenningsen (ls@emd.dk)

Co-authors: Bo H. Jacobsen (AAU)
Morten L. Thøgersen (EMD)

Motivation

Mesoscale models play increasing role in resource assessment

But mesoscale data are NOT measured 10min data

Can mesoscale data be used as is directly in energy assessments?

Contents

- Intro - Spectrum of wind variability
- Problem - too smooth mesoscale data
- Solution - correct and extrapolate spectrum
- Results
- Conclusion

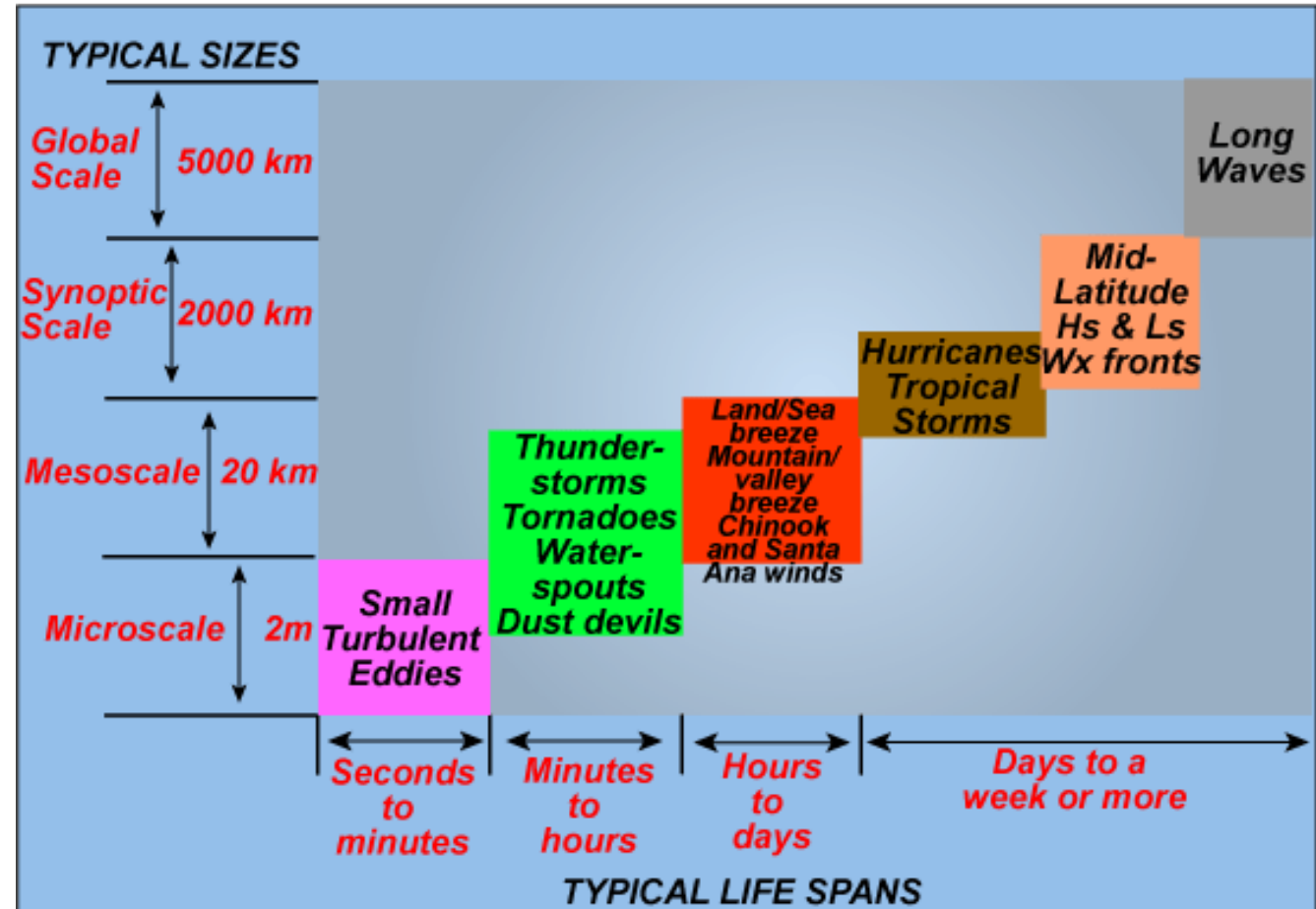
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- **Intro - Spectrum of wind variability**
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Spectrum of wind variability

Wind varies on a wide range of spatial and temporal scales

- Wind data: 10min averages



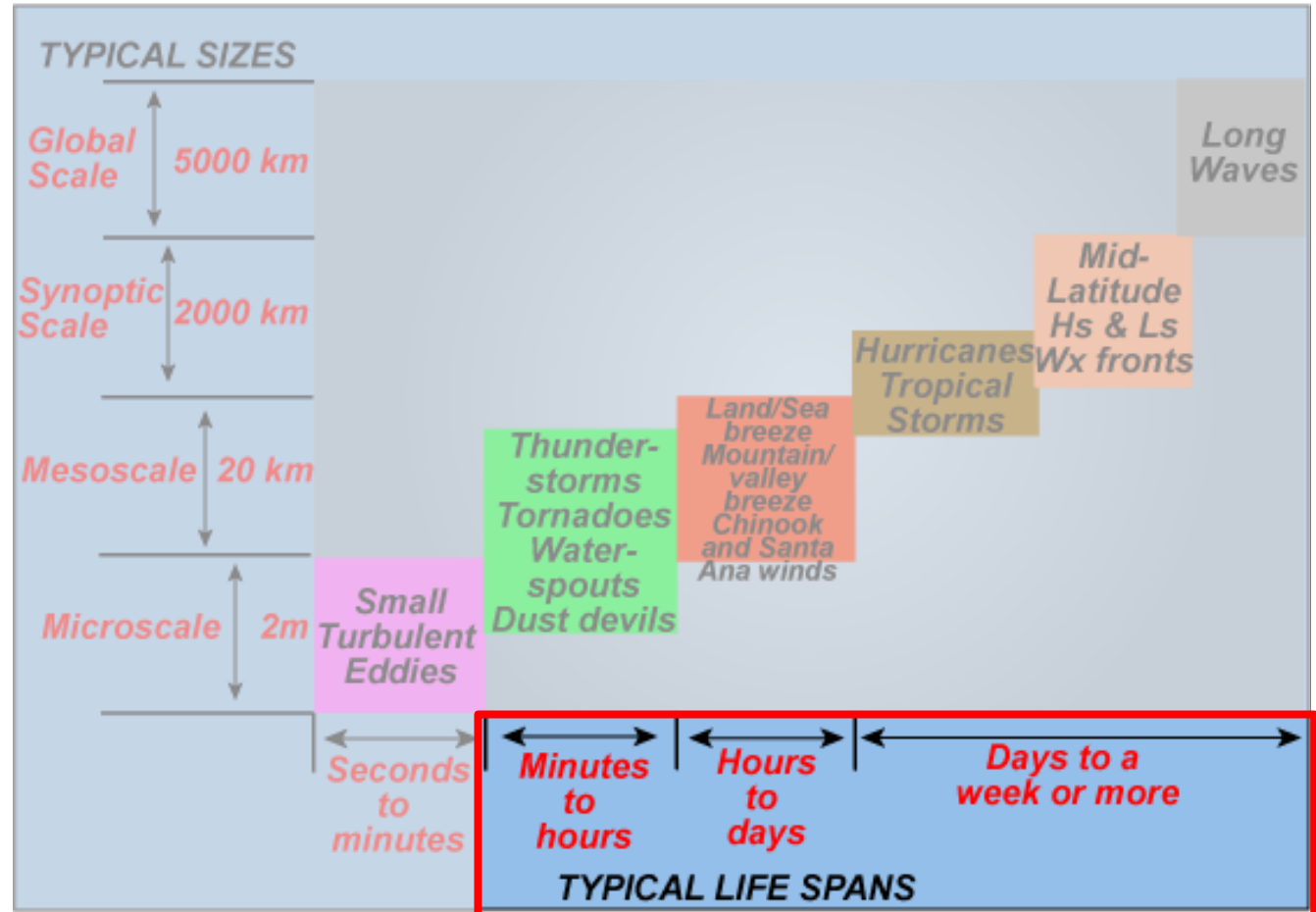
From: <http://apollo.lsc.vsc.edu/classes/met130/>

Spectrum of wind variability

Wind varies on a wide range of spatial and **temporal scales**

- Wind data: 10min averages
- Main scales 10min - 1 year:
 - Global scale (7 - 365 days)
 - Synoptic scale (2 - 7 days)
 - Mesoscale ($\frac{1}{24}$ - 2 days)
 - (Microscale) ($< \frac{1}{24}$ days)

*Stull (2000) and
Fiedler (1970)*



From: <http://apollo.lsc.vsc.edu/classes/met130/>

Spectrum of wind variability

Why is the wind variance important?

- Wind power is proportional to wind speed cubed: $P \propto u^3$
- Increased variance means more power (at same average wind speed)
- Mean wind speed is also important – but not the focus of this study

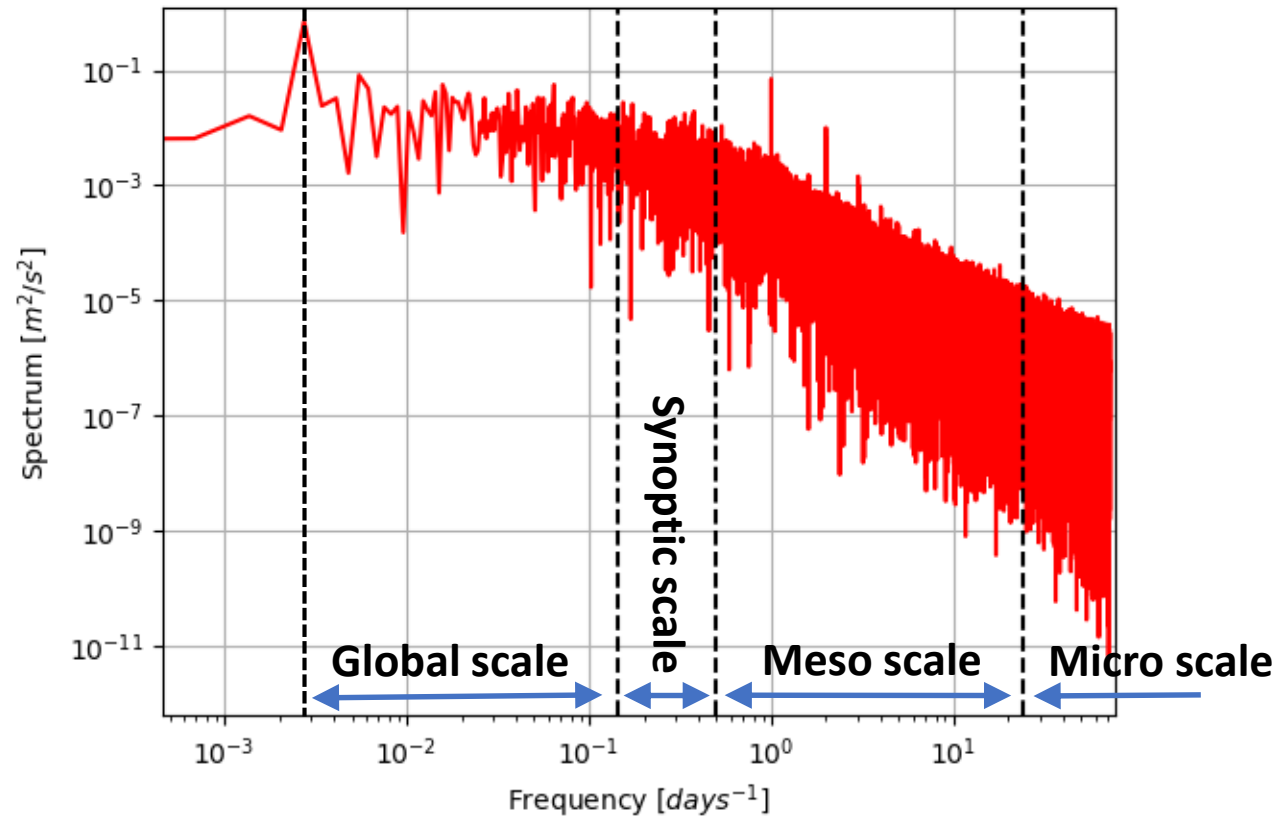
Spectrum of wind variability

What does a wind speed spectrum look like?

Spectrum of wind variability

What does a wind speed spectrum look like?

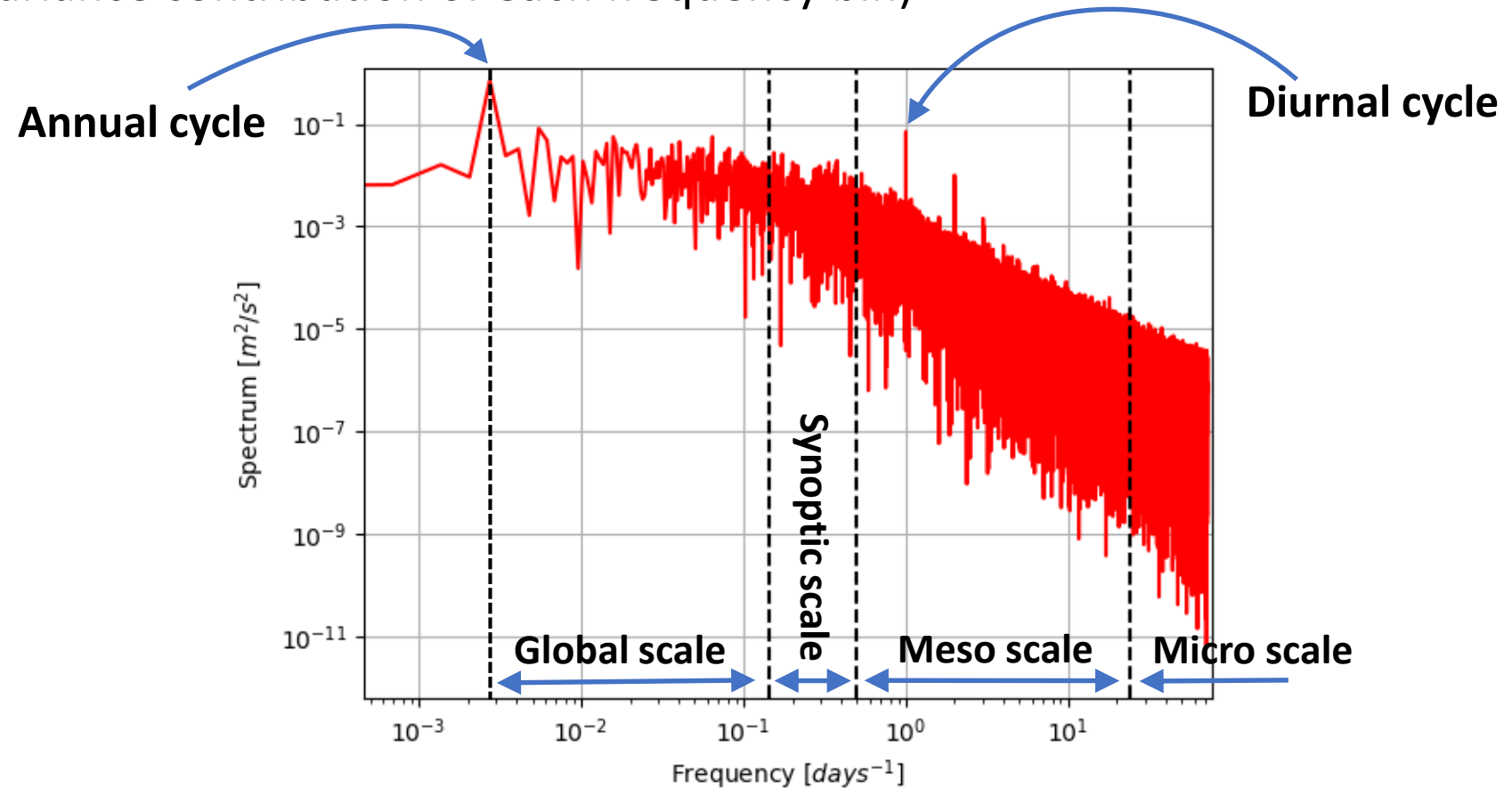
- Wind measurements - Cabauw mast (3 years, 80m agl):
- “Raw” FFT (variance contribution of each frequency bin)



Spectrum of wind variability

What does a wind speed spectrum look like?

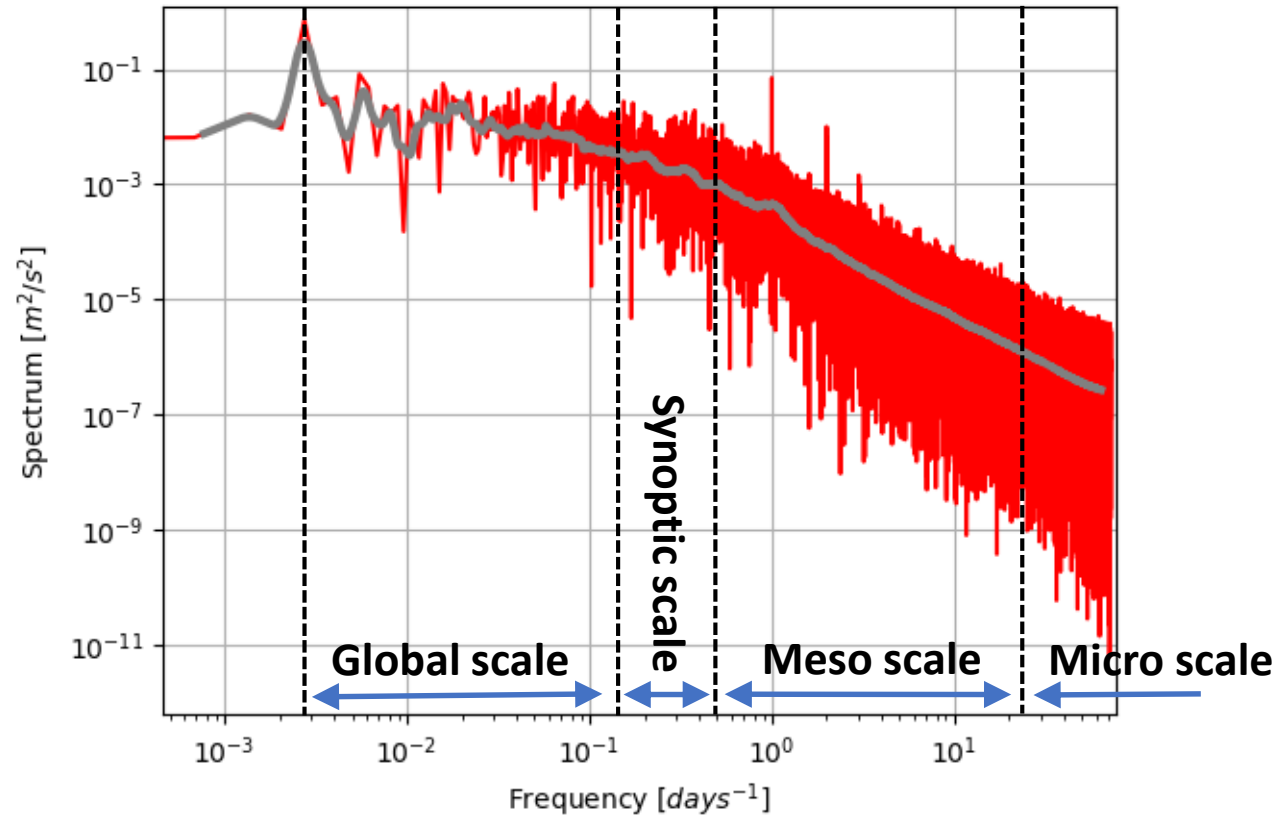
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Spectrum of wind variability

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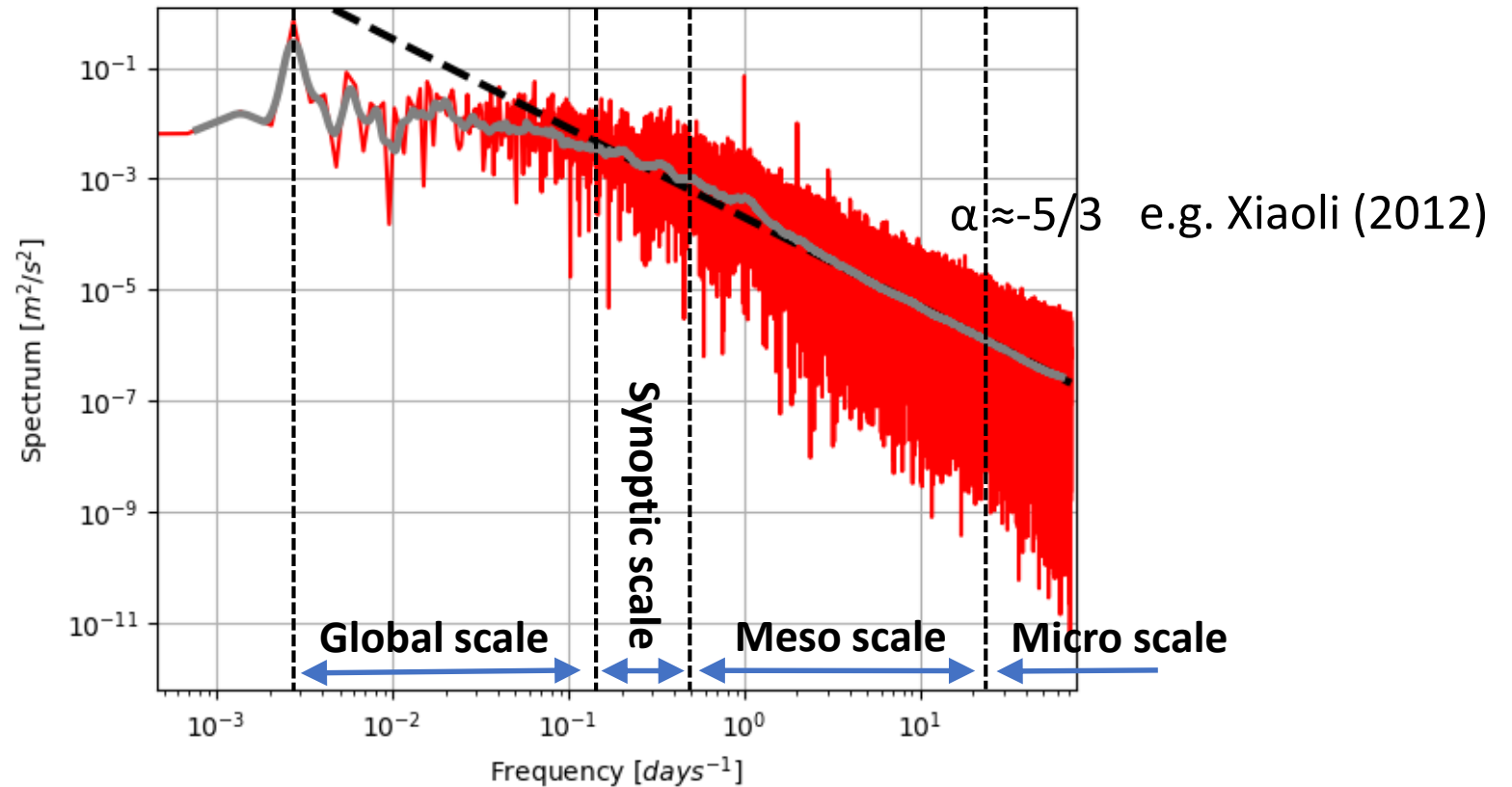
- Wind measurements - Cabauw mast (3 years, 80m agl):
- “Smoothed” FFT



Spectrum of wind variability

What does a wind speed spectrum look like?

- Wind measurements - Cabauw mast (3 years, 80m agl):
- Linear trend (log-log), $f > 1 \text{ days}^{-1}$




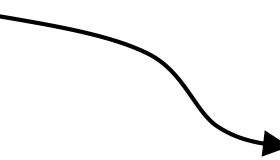
Spectrum of wind variability

Relation between spectrum and variance?

■ Variance = integral of $S(f)$ for all f \longrightarrow $\sigma^2 = \int_{f_{min}}^{f_{max}} S(f) df$

Spectrum of wind variability

Relation between spectrum and variance?

- Variance = integral of $S(f)$ for all f 
- Cumulative Spectrum = integral of $S(f)$ up to f_0 

$$\sigma^2 = \int_{f_{min}}^{f_{max}} S(f) df$$

$$\sigma_{Cum}^2(f_0) = \int_{f_{min}}^{f_0} S(f) df$$

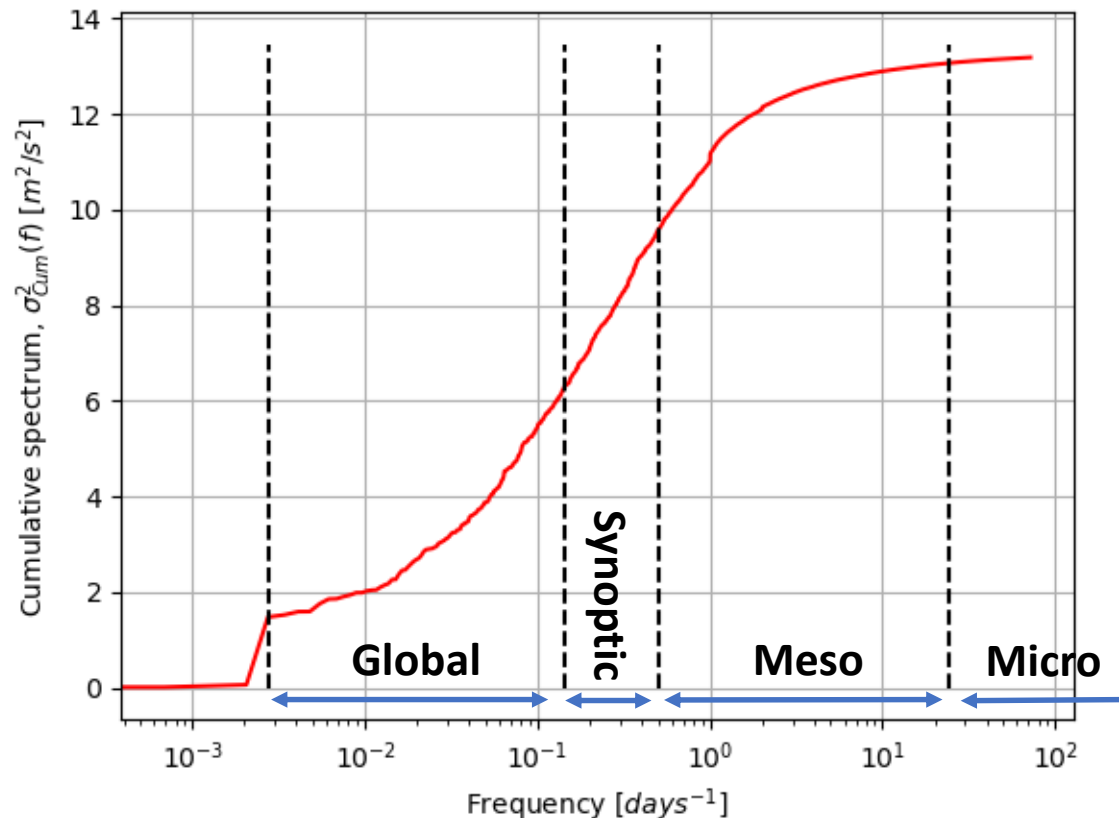
Spectrum of wind variability

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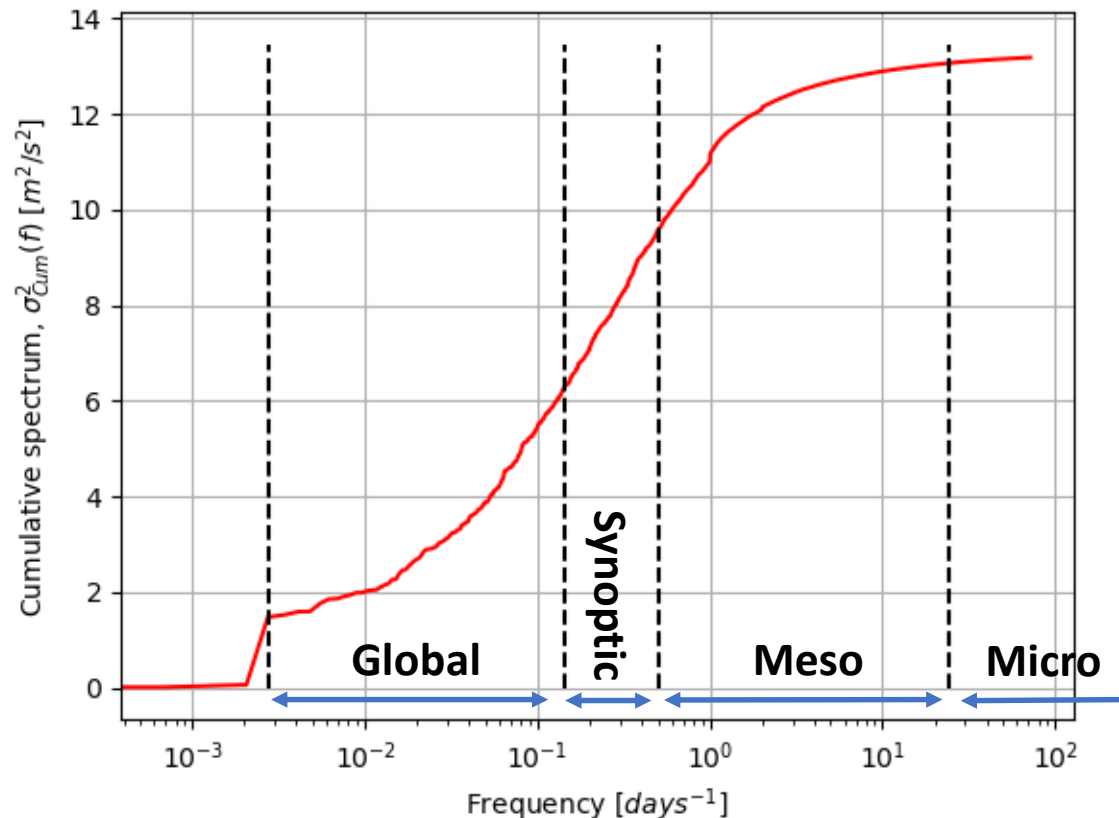
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**Note: No smoothing applied!
Just integration**

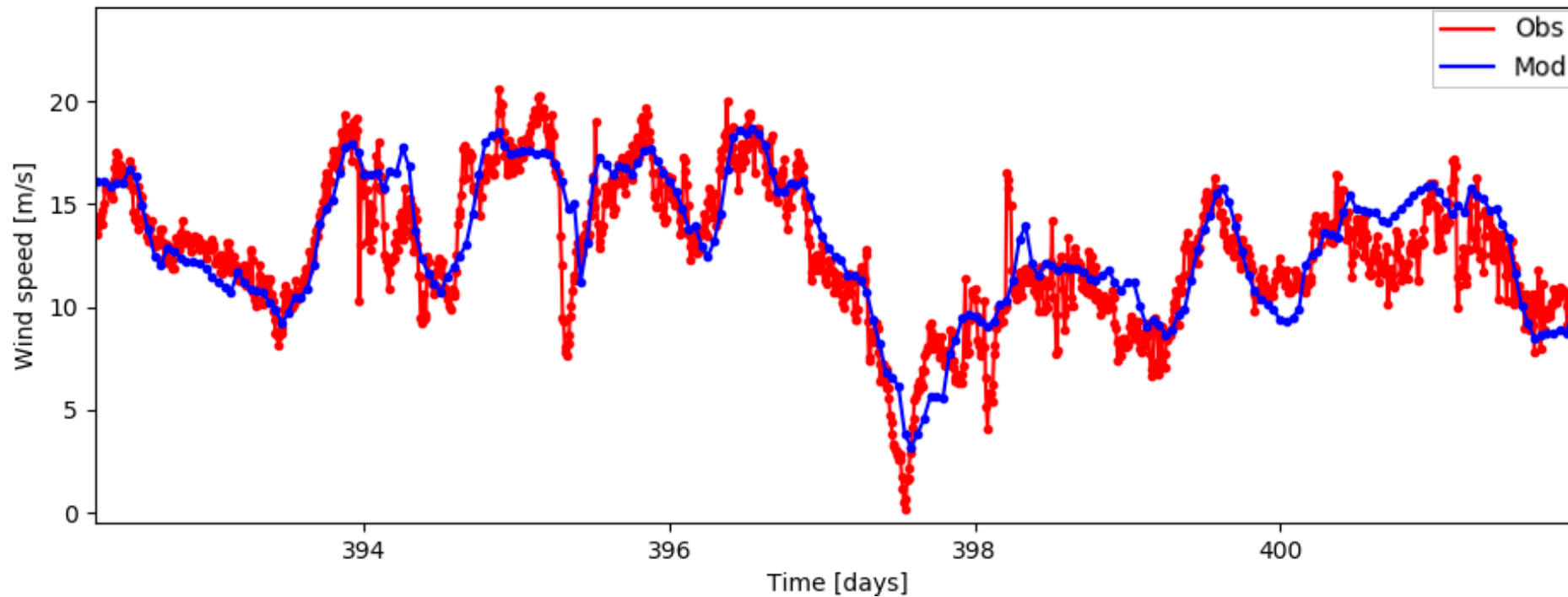
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The problem

Mesoscale model problems – **time domain**

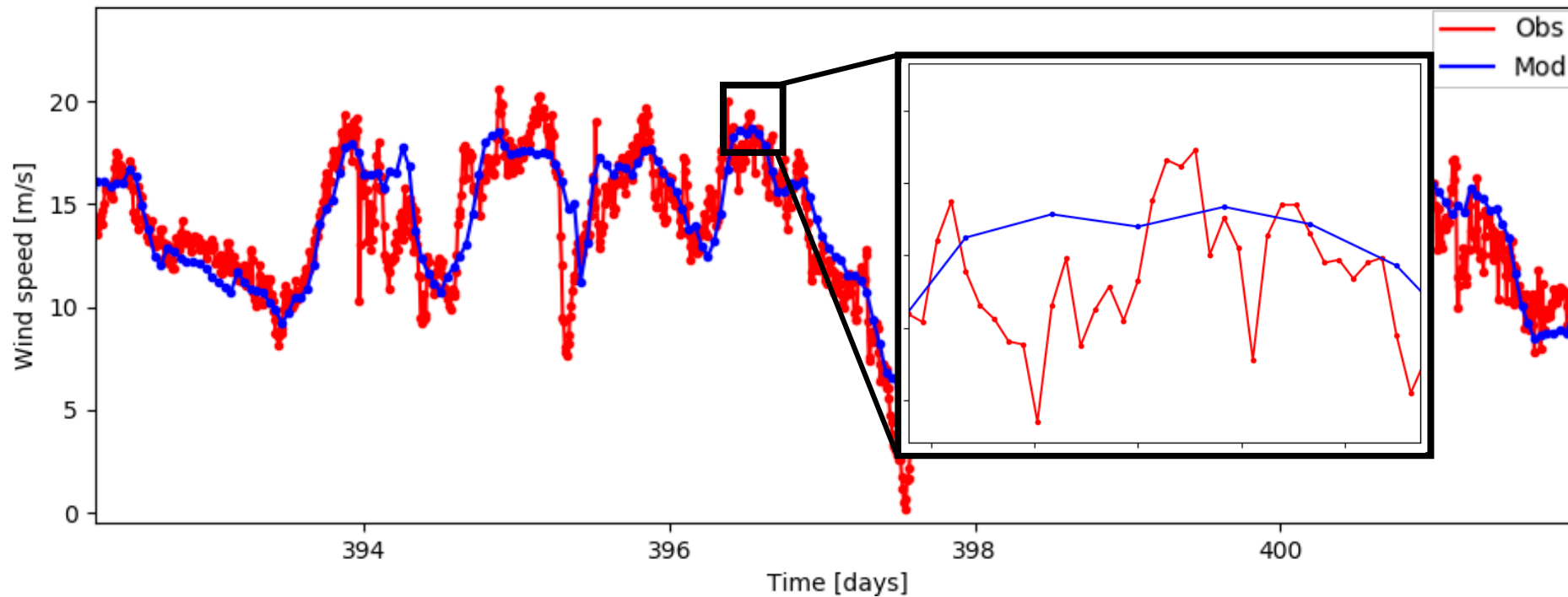
- Model data too smooth compared to measurements



The problem

Mesoscale model problems – **time domain**

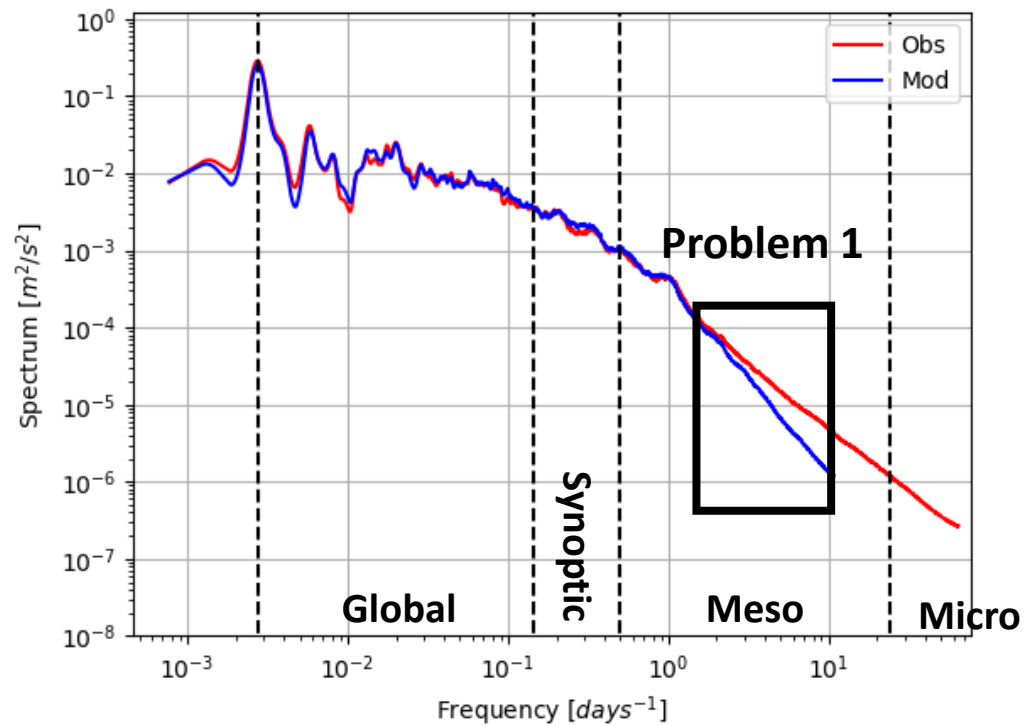
- Model data too smooth compared to measurements
- Model data (often) sampled hourly, but measurements 10min



The problem

Mesoscale model problems – frequency domain (spectrum)

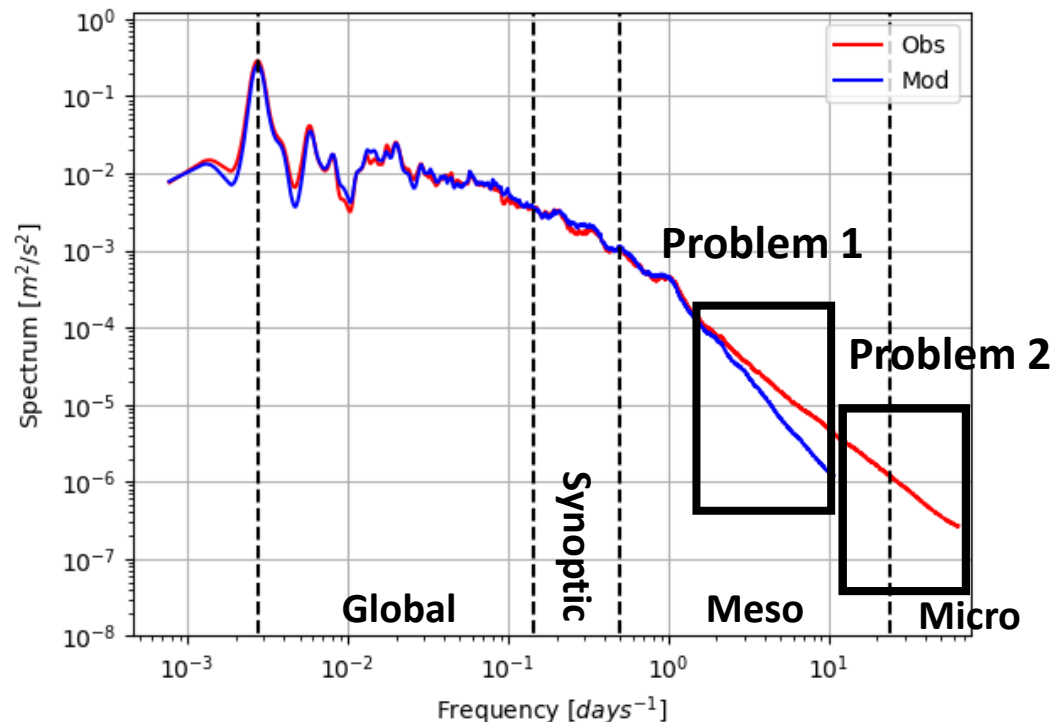
- Problem 1: Spectrum may have too high damping at high frequencies



The problem

Mesoscale model problems – frequency domain (spectrum)

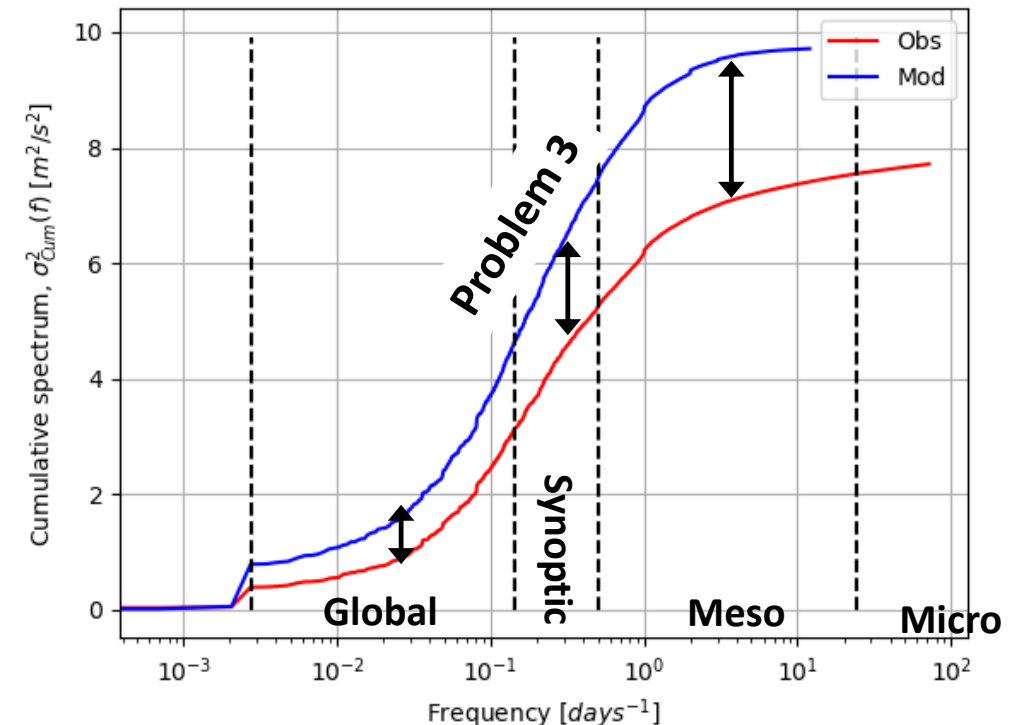
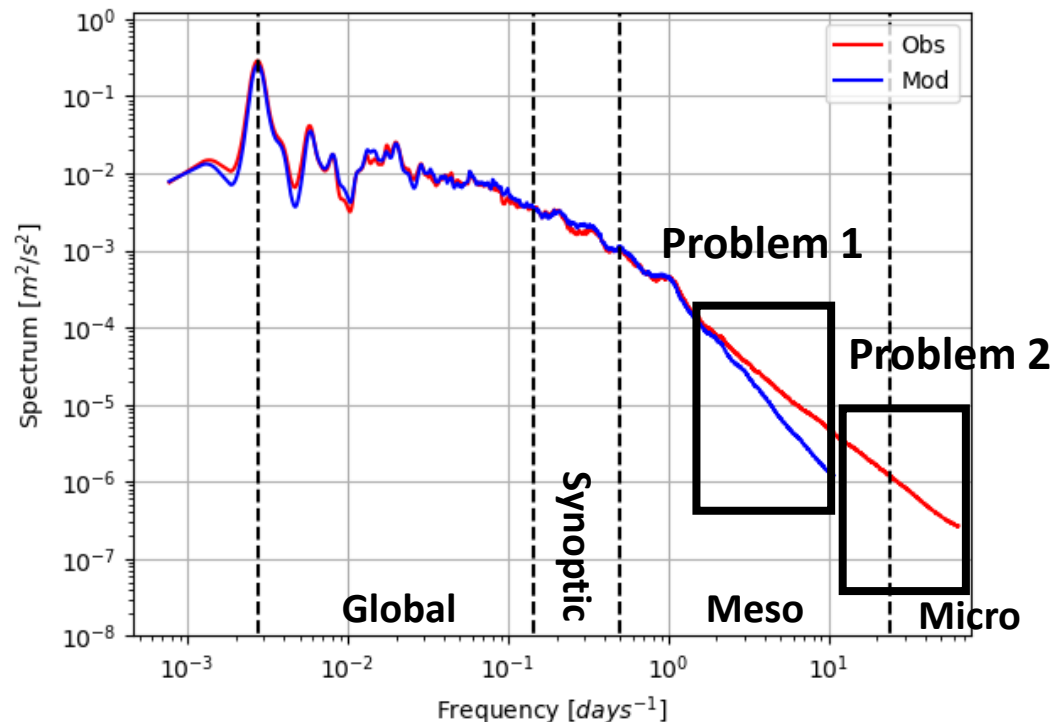
- Problem 1: Spectrum may have too high damping at high frequencies
- Problem 2: Spectrum does not cover highest frequencies (if hourly sampled)



The problem

Mesoscale model problems – frequency domain (spectrum)

- Problem 1: Spectrum may have too high damping at high frequencies
- Problem 2: Spectrum does not cover highest frequencies (if hourly sampled)
- Problem 3: Spectrum may have errors in 'main ranges' (meso, synoptic, global)



Contents

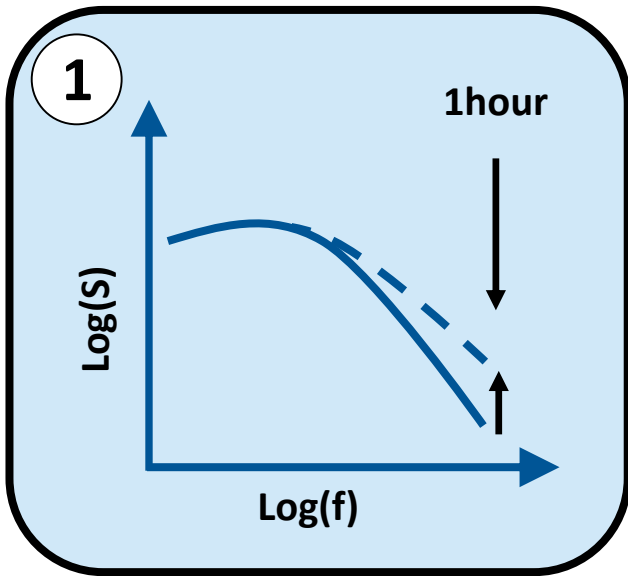
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The solution

Solution 1: Correct damping of highest frequencies

- Apply 'inverse' damping filter

(Note: not required for all mesoscale data/models, e.g. 'EMD-WRF EUR+ (ERA5)')

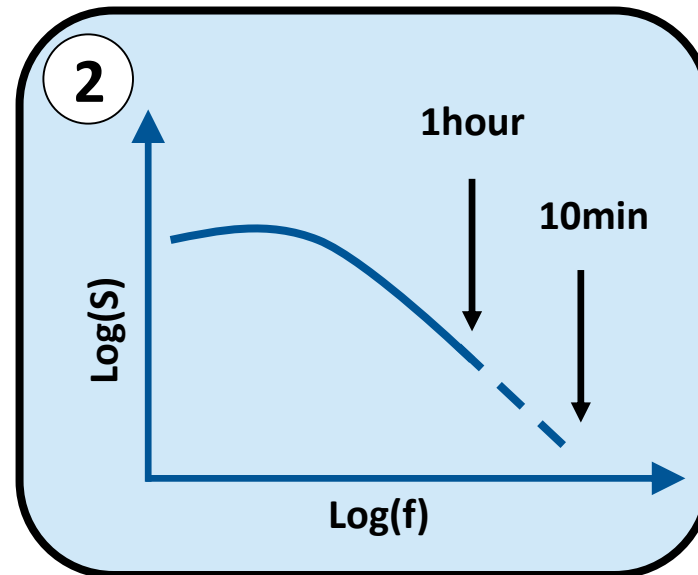
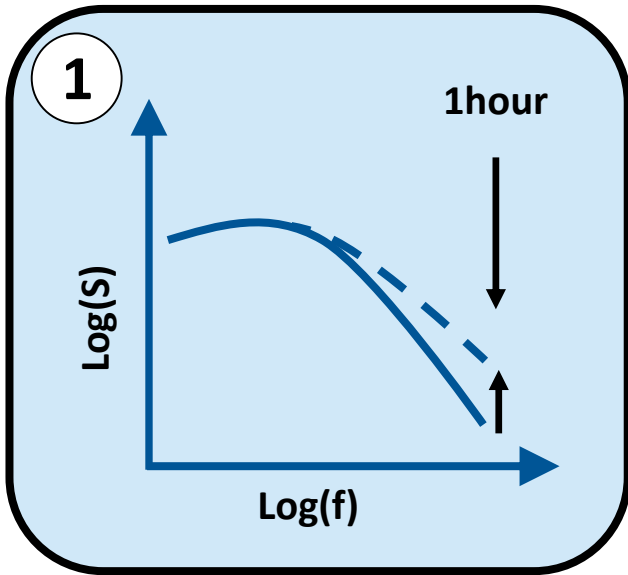


The solution

Solution 1: Correct damping of highest frequencies

Solution 2: Extrapolate spectrum to recover high frequencies

- Utilize linear nature (in log-log) to extrapolate to 10min



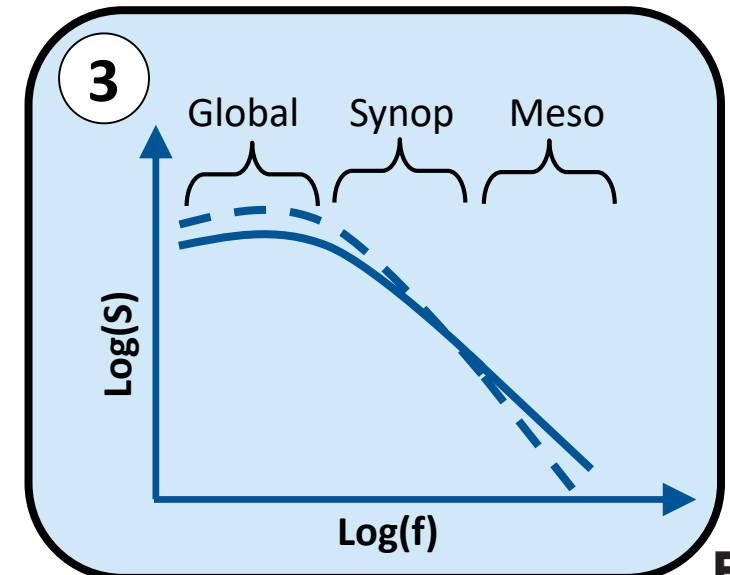
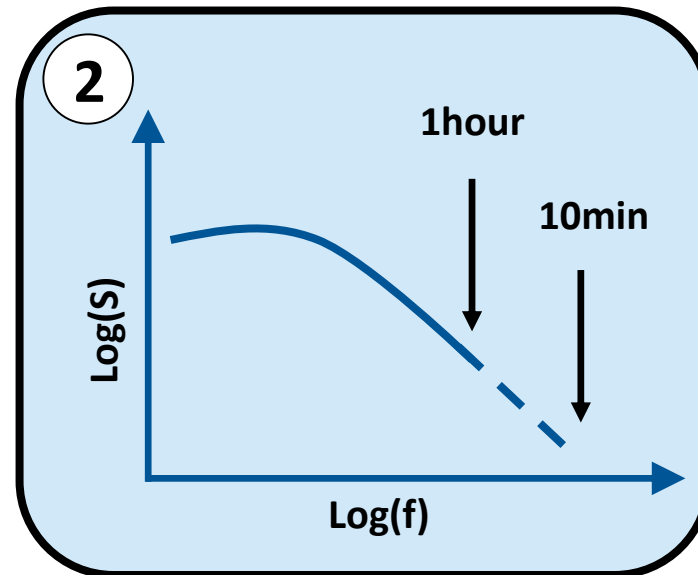
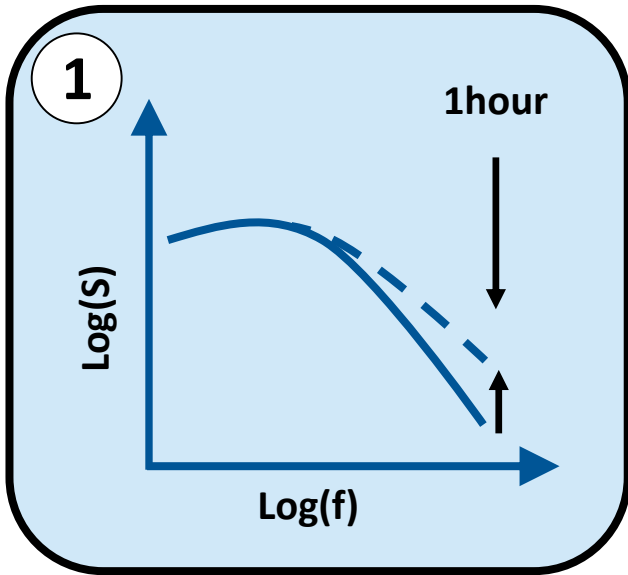
The solution

Solution 1: Correct damping of highest frequencies

Solution 2: Extrapolate spectrum to recover high frequencies

Solution 3: Correct shape of spectrum in main ranges

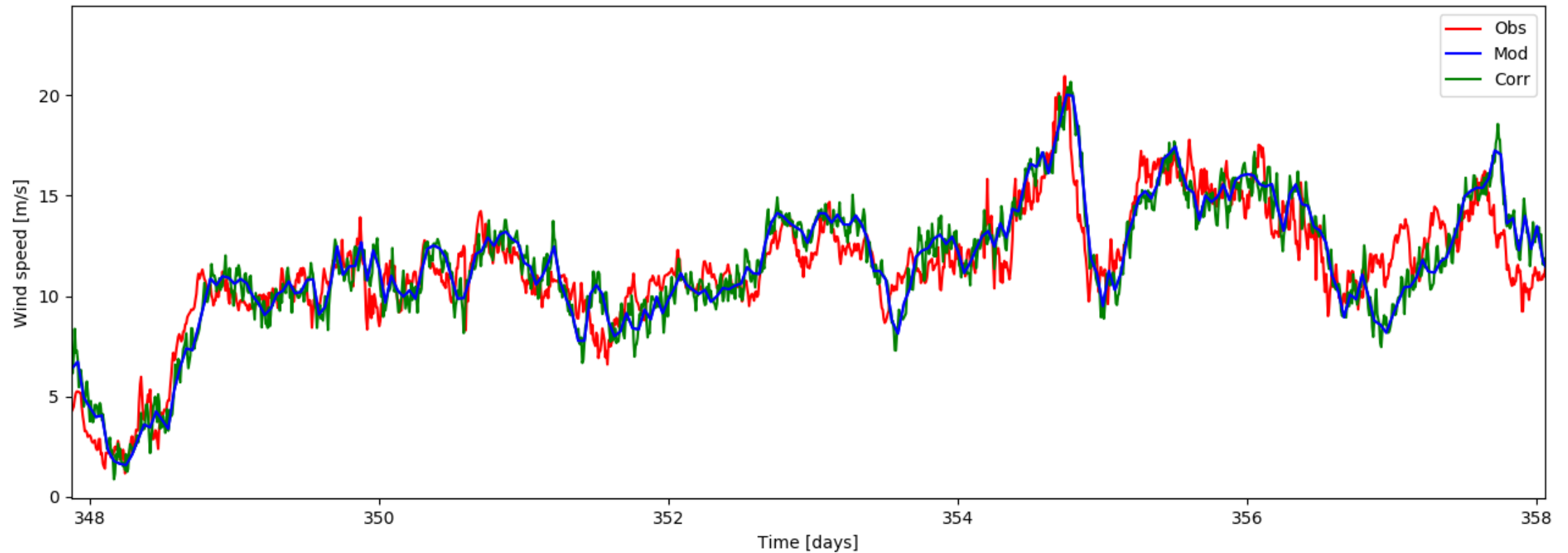
- Correct the amount of variance in each main range



The solution

Example (time domain)

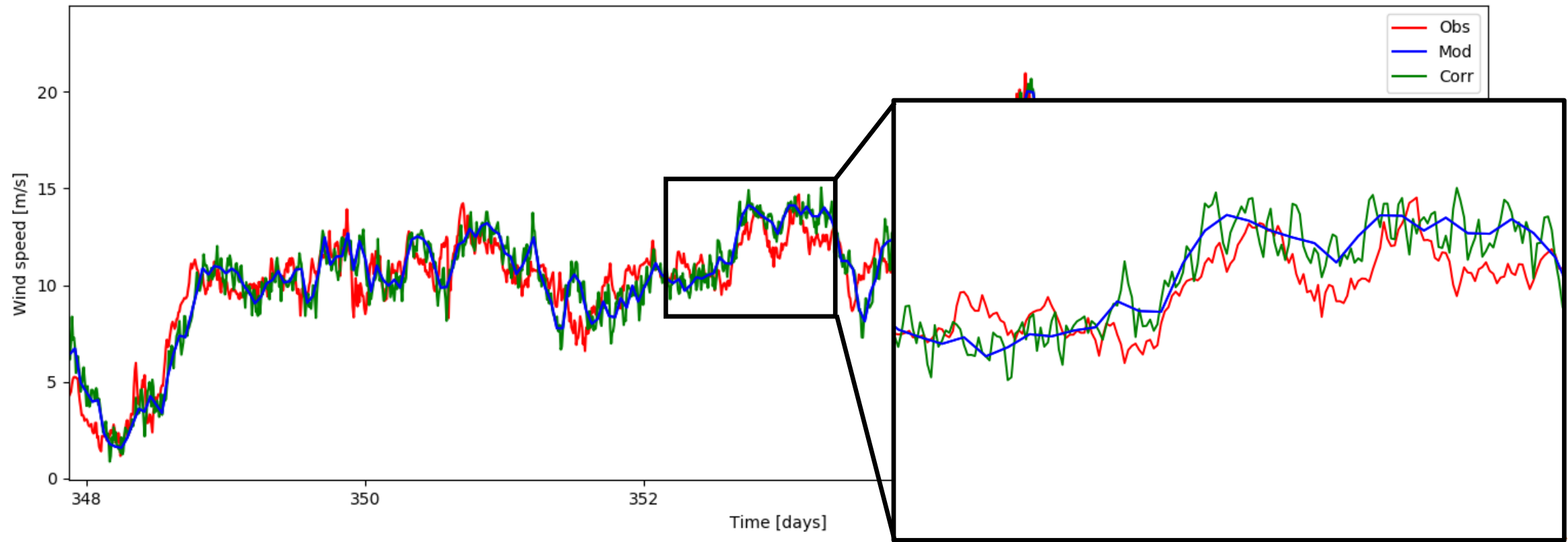
- **Obs: Cabauw** Vs **Mod: EMD-WRF Europe+** Vs **Mod+Cor. 2+3 (cor. 1 not needed)**



The solution

Example (time domain)

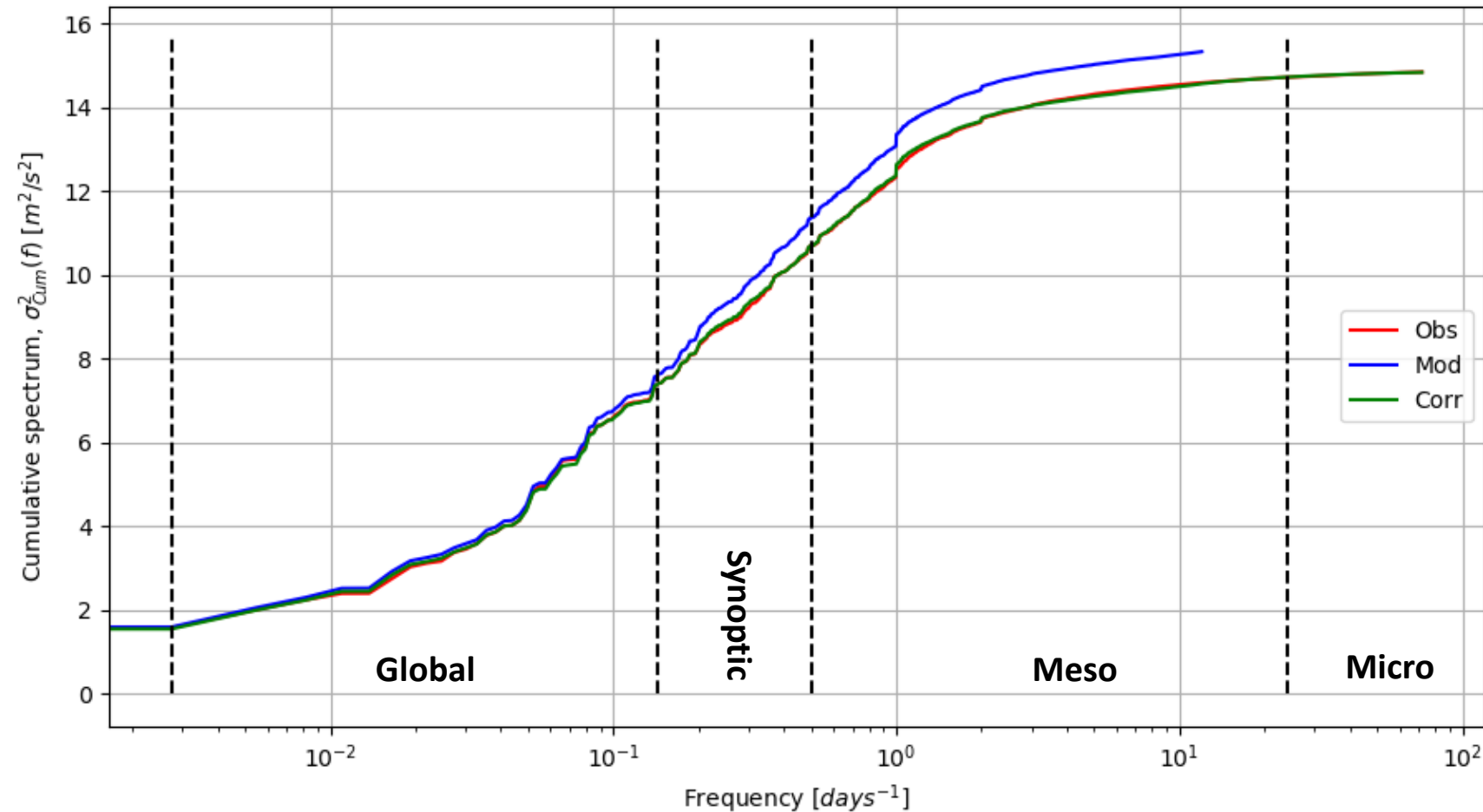
- **Obs: Cabauw** Vs **Mod: EMD-WRF Europe+** Vs **Mod+Cor. 2+3 (cor. 1 not needed)**



The solution

Example (cumulative spectrum)

- **Obs: Cabauw** Vs **Mod: EMD-WRF Europe+** Vs **Mod+Cor. 2+3 (cor. 1 not needed)**



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Results

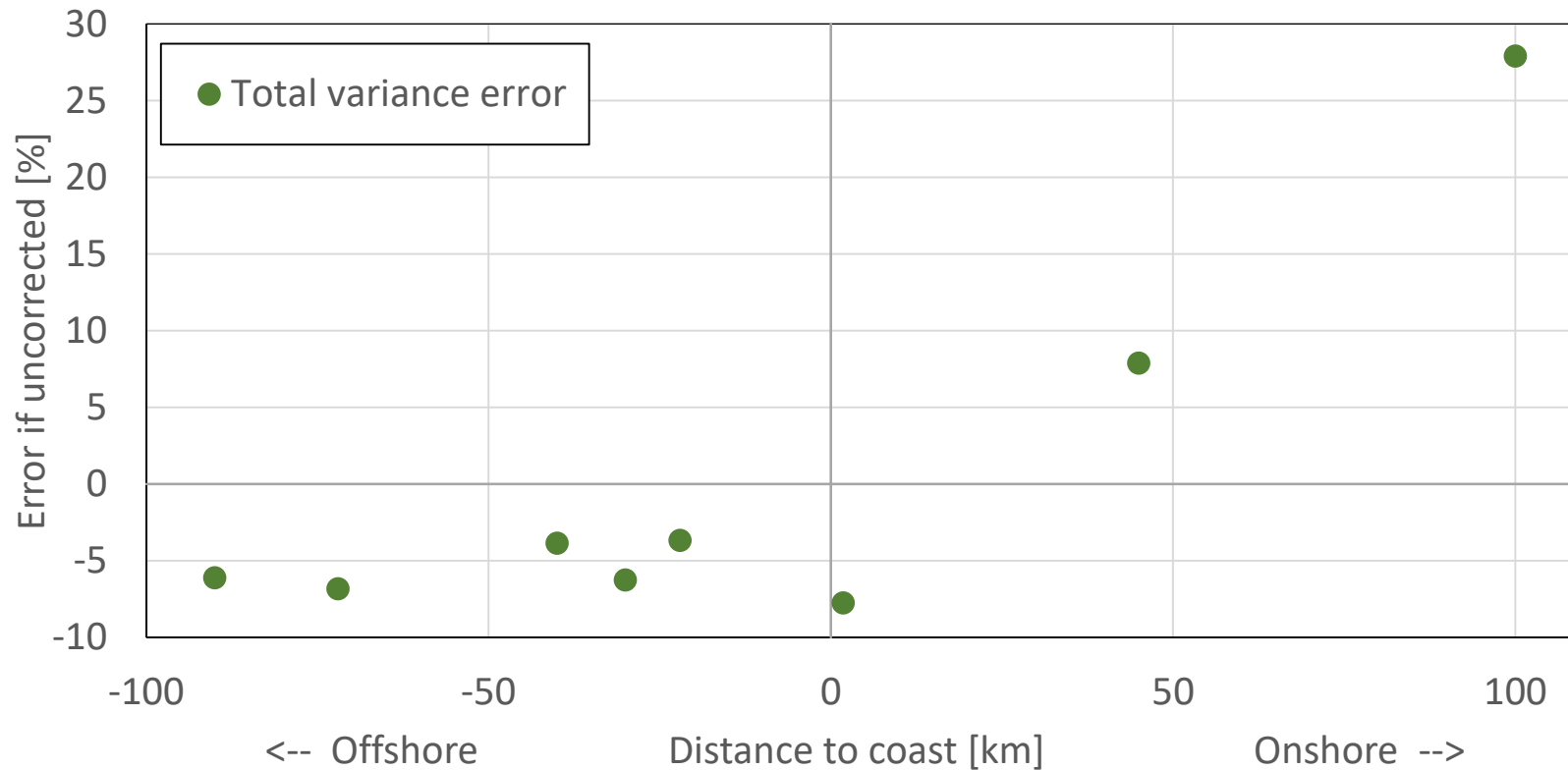
What is the effect of spectral correction?

- 8 masts from 100km offshore to 100km onshore (2-8 years)
- Errors quantified relative to corrected data to focus on spectral effects
- Hence, errors on mean wind speed are avoided

Results

What is the effect of spectral correction?

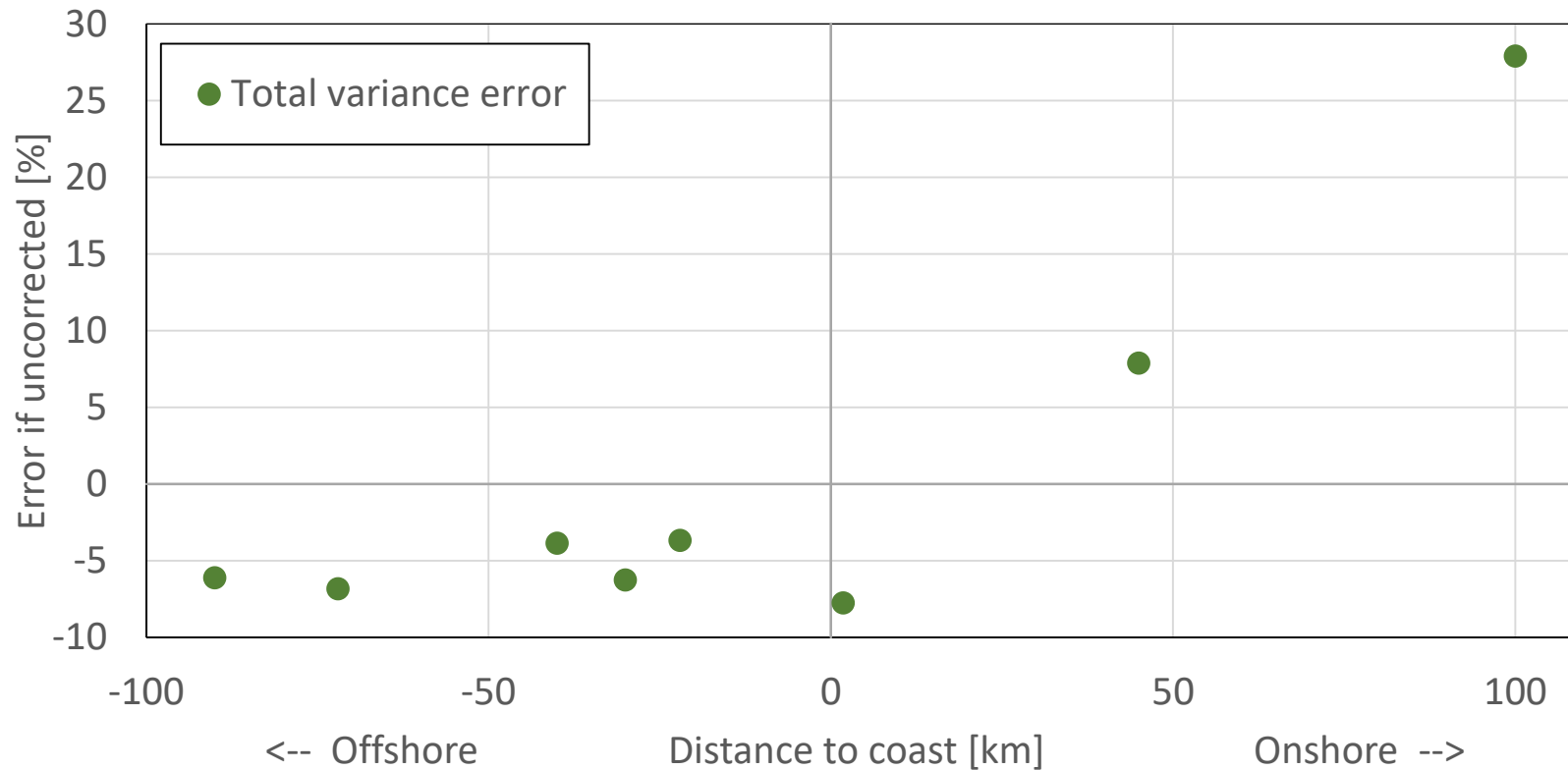
- Error on total variance (if uncorrected):



Results

What is the effect of spectral correction?

- Error on total variance (if uncorrected):



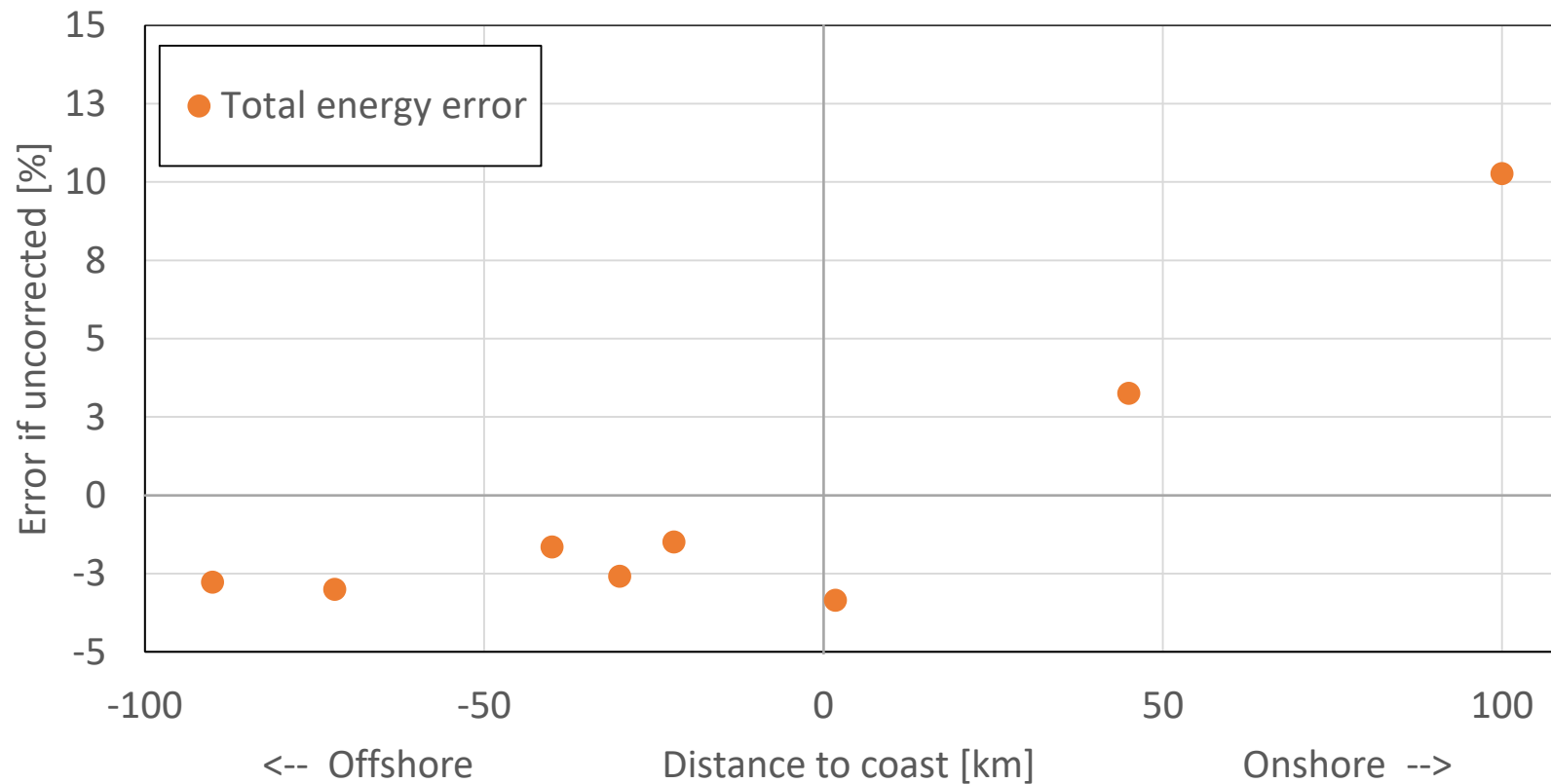
Total Variance error:

- Ca. -5% offshore
- Up to +28% onshore

Results

What is the effect of spectral correction?

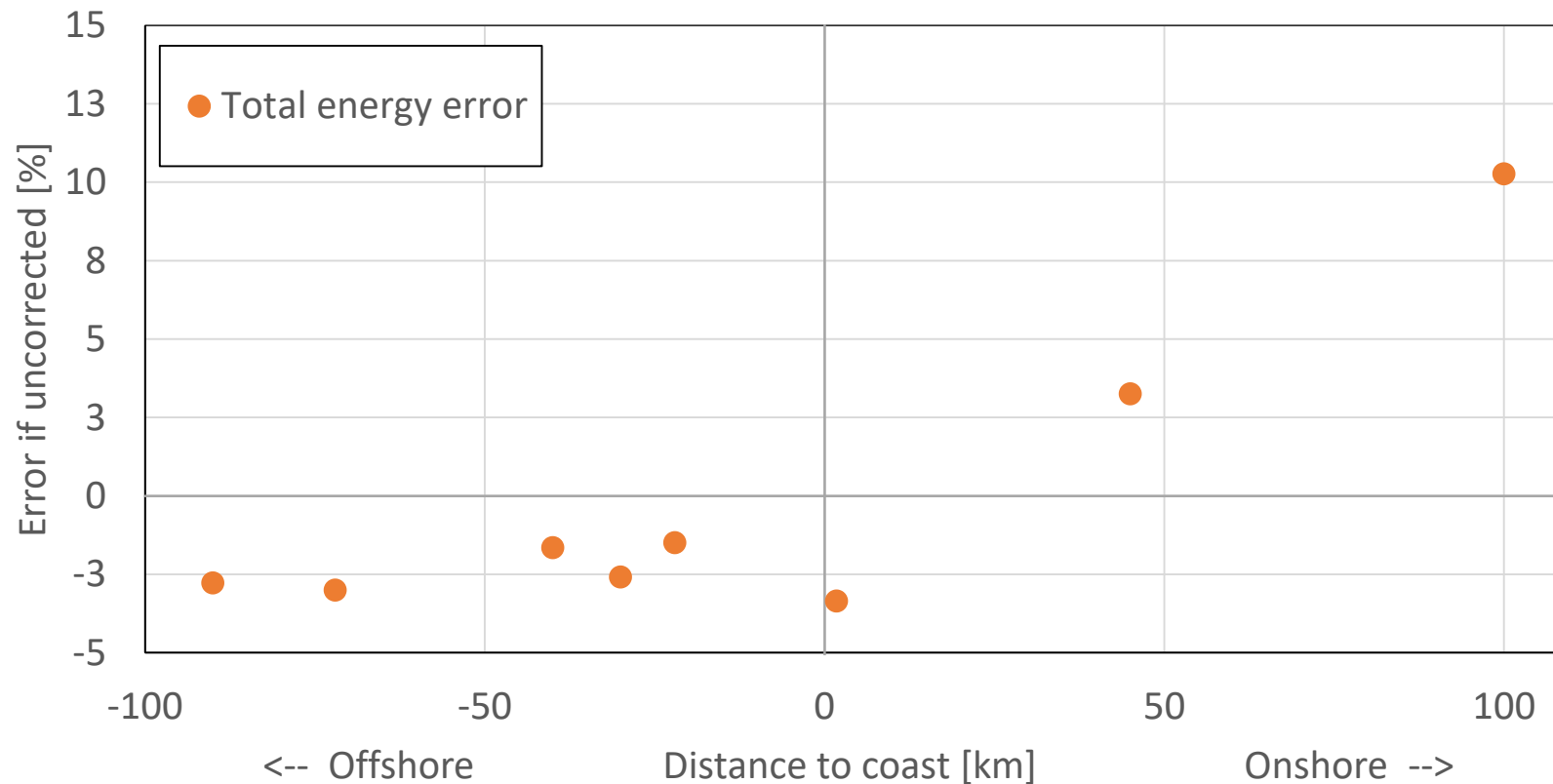
- Error on total energy $\langle u^3 \rangle$ (if uncorrected):



Results

What is the effect of spectral correction?

- Error on total energy $\langle u^3 \rangle$ (if uncorrected):
AEP error ca. 20-50% of total energy error



Total energy $\langle u^3 \rangle$ error:

- Ca. -3% offshore
- Up to +10% onshore

AEP error:

- Ca. 1% offshore
- Up to 5% onshore

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Conclusion

Spectrum of mesoscale data - summary

Problems:

- 1) Mesoscale data may be dampened too much for $f > 1 \text{ day}^{-1}$
- 2) Mesoscale data mostly sampled hourly
- 3) Mesoscale data may have erroneous variance in 'main ranges'

Conclusion

Spectrum of mesoscale data - summary

Problems:

- 1) Mesoscale data may be dampened too much for $f > 1 \text{ day}^{-1}$
- 2) Mesoscale data mostly sampled hourly
- 3) Mesoscale data may have erroneous variance in 'main ranges'

Presented solutions:

- 1) Correct damping by an applying 'inverse damping filter'
- 2) 10min samples recovered by extrapolating spectrum (linear in log-log)
- 3) Re-shape amount of variance in main ranges

Conclusion

So can mesoscale model data be used as is for AEP?

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- **onshore:**
 - **No** - spectral errors result in up to 28% error on variance and up to 5% on AEP
 - Full spectral correction recommended

Conclusion

So can mesoscale model data be used as is for AEP?

- **onshore:**
 - **No** - spectral errors result in up to 28% error on variance and up to 5% on AEP
 - Full spectral correction recommended
- **offshore:**
 - **Yes** – spectral errors result in up to 5% error on variance and up to 1% on AEP
 - **But** solution 2 is recommended to recover 10min data for consistency with 10min measurements

The End

Thanks for the attention!

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to recover full 10min variability
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Presenter:

Lasse Svenningsen (ls@emd.dk)
EMD International A/S